

Arithmetic Progression Class 10: Formulas & Examples

Use the nth-term and sum formulas for an arithmetic progression, with worked examples, a formula sheet and practice answers.

Name: _____ Date: _____

An arithmetic progression (AP) is a sequence with the same difference between every pair of consecutive terms. Before using an AP formula, subtract adjacent terms. A pattern that looks regular, such as 2, 4, 8, 16, is not an AP because its differences change.

AP formula sheet

Quantity	Formula	Meaning
Common difference	$d = a_2 - a_1$	Subtract an earlier term from the next one.
nth term	$a_n = a + (n - 1)d$	a is the first term; n counts positions starting at 1.
Sum of first n terms	$S_n = n[2a + (n - 1)d]/2$	Adds the first n terms, not the n th term alone.
Sum when last term l is known	$S_n = n(a + l)/2$	Use when n and the first and last terms are known.

Find a term and a position

The AP 7, 11, 15, ...

1. $a = 7$ and $d = 4$. The 20th term is $7 + 19 \times 4 = 83$.
2. To locate 67, solve $67 = 7 + (n - 1)4$. Then $n - 1 = 15$, so $n = 16$.
3. To test 68, the same calculation gives $n = 16.25$. Positions are positive integers, so 68 is not a term.

Find a sum

Add the first 20 terms of 7, 11, 15, ...

1. The last of these terms is 83. Pair the first and last: $7 + 83 = 90$.
2. There are 10 such pairs, so $S_{20} = 10 \times 90 = 900$.
3. The formula agrees: $20[14 + 19 \times 4]/2 = 900$.

Decreasing sequences

The AP 30, 27, 24, ...

1. $d = 27 - 30 = -3$. The tenth term is $30 + 9(-3) = 3$.
2. $S_{10} = 10(30 + 3)/2 = 165$.

3. Keep d negative throughout; do not turn a decreasing AP into an increasing one.

Practice with answers

1. Find the 15th term of 4, 9, 14, ... Answer: $4 + 14 \times 5 = 74$.

2. Find the sum of the first 12 positive multiples of 3. Answer: $3 + 6 + \dots + 36 = 12(3 + 36)/2 = 234$.

3. Is 52 a term of 5, 11, 17, ...? Answer: no; solving gives $n = 53/6$, not a positive integer.

4. A student saves ₹10 in week 1 and ₹5 more each successive week. Find the first 8 weeks' total. Answer: $8[20 + 7 \times 5]/2 = ₹220$.

Always label whether your answer is a single term or a total. The twentieth term in the first example is 83, but the sum of twenty terms is 900. Confusing a_n with S_n is a common source of otherwise correct-looking answers.

Topic reference: NCERT Mathematics, Arithmetic Progressions: <https://ncert.nic.in/textbook/pdf/jemh105.pdf>

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Read the current web version: <https://udayy.com/en/lesson/arithmetic-progression-class-10-formulas>